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Abstract - This paper proposes the speed control of brushless DC (BLDC) motor via direct power control (DPC) method as a novel and effective strategy in electrical drives applications. The DPC has some advantages rather than other control methods of BLDC motor including simpler control algorithm and faster dynamic response. In proposed BLDC motor drive based on DPC strategy, space vector modulation (SVM) voltage source inverter is employed. To enhance the drive reliability, a position sensorless strategy has been used for rotor position detection and current commutation. In developed sensorless strategy, an observer has been designed to predict the phase back-emf voltages using line voltages and currents. So, there is no need to position sensors and the cost is decreased. The performance of proposed sensorless DPC method has been verified via some simulations in Matlab under different speed and torque references.

Keywords: *Brushless DC Motor (BLDC), Direct Power Control (DPC), Sensorless Control, Drive.*

I. INTRODUCTION

In recent years, taking into consideration latest advance in permanent magnet materials, solid state devices and microelectronic have resulted in new energy efficient drives using permanent magnet brushless DC motors. BLDC motors with features such as durability, high efficiency, easier control and high power density, have found many applications in different industries such as appliances, medical, industrial automation, servo drives, automotive, aerospace, computer peripheral equipment and electric vehicles [1]. In addition to the aforementioned advantages of BLDC motors, they have high acceleration capability due to small rotor inertia and high static torque characteristics of DC motors desired function of the high velocity.

The BLDC motor is similar with the permanent magnet synchronous motor in the structure and linear torque to current, or speed to voltage similar with DC motor. Then, variable speed operation and control are easier than other AC machines. Thus, given the undeniable benefits of permanent-magnet motor and increasing progress and improve engine operating characteristics of BLDC, the need to develop and improve the control performance of BLDC motor drives can be felt.

Control of BLDC motors can be done using various techniques. The most popular way to control BLDC motors is dc link current control. This method has a simple structure. Direct torque control (DTC) is another method which is in the space vector control category because they utilize both magnitude and angular position of space vectors of motor's voltage and flux. Comparing to conventional vector controlled drives; DTC possesses several advantages such as elimination of coordinate transformation, lesser parameter dependence and faster dynamic response [2]. The latest developed technique is direct power control (DPC). Most of presented methods for power control of BLDC machines are based on current control and using PI or hysteresis current regulators as internal loops [3].

During two last decades, direct power control has been a research topic in control of electrical machines. Direct power control is a control method that directly selects output voltage vector states based on the power and flux errors using hysteresis controllers and without using current loops. In this respect, it is similar to the well know direct torque control (DTC) method described in the literatures for various AC motors [4] and lately for BLDC motors [5]. DPC technique basically is applied to generators, but it has been tried to employ it to control of electrical motors instead of DTC technique, due to problems of torque estimation and dependency to the motor's parameters in DTC. Therefore, DPC technique enjoys all advantages of DTC such as fast dynamic and ease of implementation, without having the DTC's problems. To control the motor, the rotor angle is necessary to be known. On the other hand, reducing the manufacturing cost of BLDC motor drives is an attractive issue in commercial applications. It can be reduced more by elimination of position sensors and developing feasible sensorless methods. Furthermore, sensorless control is the only choice for some applications where these sensors cannot function reliably because of the harsh environments.

In this study, the direct power control for BLDC motors will be used. The paper is organized as follows; section II gives an overview of the BLDC motor drive and its modeling, DPC strategy and employing it for BLDC motor is presented in section III. The proposed sensorless control method is given in Section IV. Simulation results are presented in section V to demonstrate the performance of the proposed control strategy and finally conclusions are given in section VI.

II. BRUSHLESS DC MOTORS

Brushless dc motor consists of a permanent magnet, which rotates (the rotor), surrounded by three equally spaced windings, which are fixed (the stator). Current flow in each winding produces a magnetic field vector. By controlling currents in the three windings, a magnetic field of arbitrary direction and magnitude can be produced by the stator.

The BLDC motor drive block diagram is shown in Fig. 1. Assuming that the stator resistances of all the windings are equal and also self and mutual inductances are constant, the voltage equation of the three phases can be expressed as (1). In this equation, magnets, stainless steel retaining sleeves with high resistivity, and rotor-induced currents are neglected and damper windings are not modeled [6].

$$\begin{bmatrix} e_{an} \\ e_{bn} \\ e_{cn} \end{bmatrix} = \begin{bmatrix} R & 0 & 0 \\ 0 & R & 0 \\ 0 & 0 & R \end{bmatrix} \begin{bmatrix} i_a \\ i_b \\ i_c \end{bmatrix} + \begin{bmatrix} L_s - M & 0 & 0 \\ 0 & L_s - M & 0 \\ 0 & 0 & L_s - M \end{bmatrix} \frac{d}{dt} \begin{bmatrix} i_a \\ i_b \\ i_c \end{bmatrix} + \begin{bmatrix} v_{an} \\ v_{bn} \\ v_{cn} \end{bmatrix} \quad (1)$$

where R_s , L_s , M are the resistance, inductance and mutual inductance of the stator and v , e and i are phase voltage, back emf voltage and phase current of the stator respectively [7]. BLDC motor has characteristics like a DC motor, whereas it is controlled the same as AC motors.

III. DIRECT POWER CONTROL OF BLDC MOTOR

The main issue in DPC is the correct calculation of the power. If the stator winding loss and core loss are small enough to be neglected, the input electrical power is the same as the electromagnetic power. If also the rotational losses are small and negligible, the electrical input power can be approximated as the mechanical output power. Thus,

$$P_{in} \cong P_e = P_{out} \quad (2)$$

where, P_{in} , P_e and P_{out} represent the electrical input power, the electromagnetic power and the mechanical output power, respectively. The mechanical input power can be expressed as:

$$P_{in} = T_{em} \frac{\omega_r}{p} \quad (3)$$

The electromagnetic torque of a BLDC motor in the synchronously rotating d-q reference frame can be expressed by [8]:

$$T_{em} = \frac{3P}{4} \left[\left(\frac{dL_{ds}}{d\theta_e} i_{sd} + \frac{d\varphi_{rd}}{d\theta_e} - \varphi_{sq} \right) i_{sd} + \left(\frac{dL_{qs}}{d\theta_e} i_{sq} + \frac{d\varphi_{rq}}{d\theta_e} + \varphi_{sd} \right) i_{sq} \right] \quad (4)$$

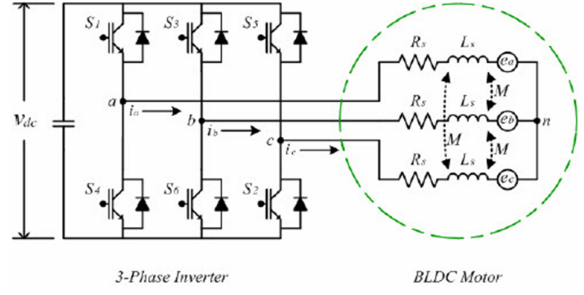


Figure 1. Three-phase equivalent circuit for BLDC motor

Substituting the torque in (3) with (4) the output power becomes:

$$P_{out} = \frac{3\omega_r}{4} \left[\left(\frac{dL_{ds}}{d\theta_e} i_{sd} + \frac{d\varphi_{rd}}{d\theta_e} - \varphi_{sq} \right) i_{sd} + \left(\frac{dL_{qs}}{d\theta_e} i_{sq} + \frac{d\varphi_{rq}}{d\theta_e} + \varphi_{sd} \right) i_{sq} \right] \quad (5)$$

θ_e is the rotor electrical angle, p is the number of poles, i_{sd} , i_{sq} are d and q-axes currents, L_{ds} , L_{qs} are d and q-axes stator inductances, and φ_{rd} , φ_{rq} , φ_{sd} and φ_{sq} are d and q-axes rotor and stator flux linkages, respectively. If L_{ds} and L_{qs} be constant, then (5) can be rewritten as:

$$P_{out} = \frac{3\omega_r}{4} \left[\left(\frac{d\varphi_{rd}}{d\theta_e} - \varphi_{rd} \right) i_{sd} + \left(\frac{d\varphi_{rq}}{d\theta_e} + \varphi_{rq} \right) i_{sq} + (L_{ds} - L_{qs}) i_{sd} i_{sq} \right] \quad (6)$$

For the non-salient-pole rotor there is:

$$L_{sd} = L_{sq} \quad (7)$$

The flux linkages and stator currents in the stationary $\alpha - \beta$ reference frame can be expressed as:

$$\varphi_{r\alpha} = \varphi_{rd} \cos \theta_e - \varphi_{rq} \sin \theta_e \quad (8)$$

$$\varphi_{r\beta} = \varphi_{rd} \sin \theta_e + \varphi_{rq} \cos \theta_e \quad (9)$$

$$i_{s\alpha} = i_{sd} \cos \theta_e - i_{sq} \sin \theta_e \quad (10)$$

$$i_{s\beta} = i_{sd} \sin \theta_e + i_{sq} \cos \theta_e \quad (11)$$

and the power equation can be simplified as:

$$P_{out} = -\frac{3\omega_r}{2} \frac{1}{2} \left[\frac{d\varphi_{r\alpha}}{d\theta_e} i_{s\alpha} + \frac{d\varphi_{r\beta}}{d\theta_e} i_{s\beta} \right] = -\frac{3\omega_r}{2} \frac{1}{2} \left[\frac{e_{\alpha}}{\omega_e} i_{s\alpha} + \frac{e_{\beta}}{\omega_e} i_{s\beta} \right] \quad (12)$$

where, e_{α} and e_{β} are back-emf obtained from the look up table. The electromagnetic torque produced in motor is:

$$T_{em} = \frac{2}{3} p \text{Im}(i_s \varphi_s^*) \quad (13)$$

Substituting the torque in (3) with (13), the real output power becomes:

$$P_{out} = \frac{2\omega_r}{3} \text{Im}(i_s \varphi_s^*) = \frac{2}{3} \frac{\omega_r}{L_s} \varphi_s \varphi_r \sin(\theta_s - \theta_r) \quad (14)$$

Since the magnitude of the stator flux is kept constant and the rotor flux does not change much due to its inertia, the rotor speed and angle can be considered constant too.

The formula above shows that the change of output power depends only on the change of stator voltage angle. The stator voltage vector that can increase the stator angle needs to be raised in order to increase the output power. The real output power equation obtained above is only valid explanation of the

principles of power control. However, it is not appropriate for the purpose of estimating the actual power in simulations. The demand power is controlled via hysteresis controller type that has two level output as shown in Fig. 2. The values are $bp=1$ and $bp=0$ represents an increase and a decrease of the power respectively. The task of the state selector in the direct power control is to select the required voltage vectors of the inverter.

Fig. 3 shows non-zero voltage space vectors for BLDC motor. A whole voltage cycle of 360° is divided equally into 6 sectors; each one spanning 60° . To understand more about switching mode in the DPC control structure, the reference power is assumed to be higher than the actual power, in the area- 30° to 30° (sector I) as shown in Fig. 2 that the power changes is expressed by $bp=1$. In this mode, for the real power follows the reference power, V_2 should be applied. In the same manner, if the actual power value is greater than the reference power, the power changes is expressed with $bp=0$ that, in this case V_5 vector is applied to reduce the amount of the real power. Switching instructions is applied to the inverter shown in Fig. 2. According to explain above, inverter switching pattern with considering power variations is presented in the table I.

IV. PROPOSED SENSORLESS CONTROL METHOD

A BLDC motor requires an inverter and a rotor position sensor to perform commutation process because a permanent magnet synchronous motor does not have brushless and commutators in DC motors. However, the position sensor presents several disadvantages from the standpoints of drive's cost, machine size, reliability, and noise immunity. Conventional sensorless control methods can be classified into several categories. Some of these methods are given below:

In the first category, the open phase current sensing method [9] is a technique for detecting the conducting interval of freewheeling diodes connected in antiparallel with power transistors. Secondly, the method detecting the third harmonic of back-emf [10,11] is the technique to remove all the fundamental and other poly-phase components through a simple summation of three phase voltages. Thirdly, the back-emf integrating method [12,13] is a technique applying the principle that integration is constant from Zero Crossing Point (ZCP) to 30° . Finally, the open phase voltage sensing method [14] is a scheme estimating the rotor position indirectly by using the ZCP detection of open phase's terminal voltage. In this paper, sensorless control method utilizing an unknown input observer is used. This sensorless control method incorporating an unknown input observer is independent of the rotor speed for a BLDC motor drive.

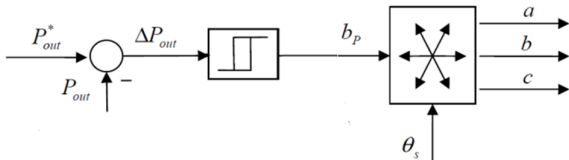


Figure 2. Block diagram of the inverter state selection

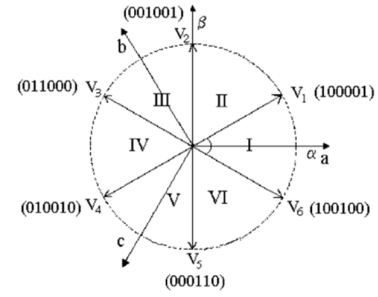


Figure 3. Non-zero voltage space vectors for BLDC motor

TABLE I. SWITCHING TABLE

b_p	Sector1	Sector2	Sector3	Sector4	Sector5	Sector6
$b_p=0$	V_2	V_3	V_4	V_5	V_6	V_1
$b_p=1$	V_5	V_6	V_1	V_2	V_3	V_4

The proposed sensorless control method in this paper is based on the fact that the rotor position can be detected by using trapezoidal back-emf of BLDC motors [15]. Since a back-emf of the BLDC motor is not measured directly, it is estimated by the unknown input observer. This unknown input observer is constructed by a back-emf regarded as an unknown input and state of the BLDC motor drive system. The sensorless control method using the unknown input observer can be obtained as follows: First line-to-line back-emf estimation using the unknown input observer since the neutral point of the BLDC motor is not offered, it is difficult to construct the equation for one phase. Therefore, the unknown input observer is considered by the following line-to-line equation:

$$\frac{di_{ab}}{dt} = -\frac{2R_s}{2L}i_{ab} + \frac{1}{2L}v_{ab} - \frac{1}{2L}e_{ab}. \quad (15)$$

In (15) i_{ab} and v_{ab} can be measured, therefore they "known" state variables. On the other hand, since e_{ab} cannot be measured, this term is considered as an unknown state. Equation 15 can be rewritten in the following matrix form:

$$\frac{dx}{dt} = Ax + Bu + Fw. \quad (16)$$

$$y = cx. \quad (17)$$

where

$$A = \left[-\frac{2R_s}{2L} \right], B = \left[\frac{1}{2L} \right], F = \left[-\frac{1}{2L} \right] \quad (18)$$

$$x = [i_{ab}], u = [v_{ab}], w = [e_{ab}], y = [i_{ab}], C = [1] \quad (19)$$

The back-emf is regarded as an unknown disturbance and can be represented by a differential equation:

$$\frac{dz}{dt} = Dz. \quad (20)$$

$$w = Hz. \quad (21)$$

where

$$D = \begin{bmatrix} 0_{(\delta-1) \times 1} & I_{(\delta-1)} \\ 0_{1 \times 1} & 0_{1 \times (\delta-1)} \end{bmatrix}, \quad H = \begin{bmatrix} I_1 & 0_{1 \times (\delta-1)} \end{bmatrix} \quad (22)$$

I is identity matrix and δ is degree of polynomial expression under:

$$w = \sum_{i=0}^{\delta} a_i t^i, \quad \delta \geq 1. \quad (23)$$

where a_i denotes a set of unknown coefficient vectors. In cases of no experimental information about disturbance, a_i can be defined as $a_i = 0$. The entire system can be expressed by the augmented equation observer that introduces disturbances of differential equation form modeling the back-emf. The augmented model can be shown as (24) and (25):

$$\frac{dx_a}{dt} = A_a x_a + B_a u. \quad (24)$$

$$y = C_a x_a. \quad (25)$$

where

$$A_a = \begin{bmatrix} -\frac{2R_s}{2L} & -\frac{1}{2L} \\ 0 & 0 \end{bmatrix}, x_a = \begin{bmatrix} i_{ab} \\ e_{ab} \end{bmatrix}, B_a = \begin{bmatrix} \frac{1}{2L} \\ 0 \end{bmatrix}, \quad (26)$$

$$u = [v_{ab}], y = [i_{ab}], C_a = [1 \ 0].$$

The degree of polynomial expression for disturbance is established by $\delta = 1$. Since, the system displayed by (24) and (25) is observable, it is possible to compose the following observer:

$$\frac{d\tilde{x}_a}{dt} = A_a \tilde{x}_a + B_a u + K(y - \tilde{y}). \quad (27)$$

K is the gain matrix of the observer [12]. If the gain of the observer is selected properly, this observer can accurately estimate line-to-line currents and back-emfs of the motors [16]. Fig. 4 shows a block diagram of the proposed back-emf observer.

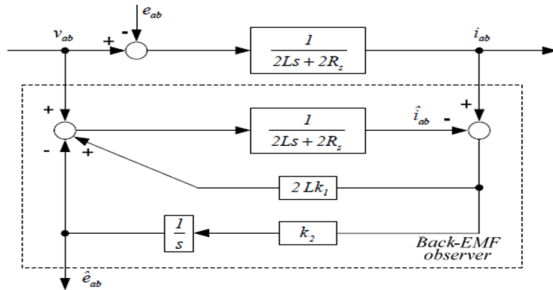


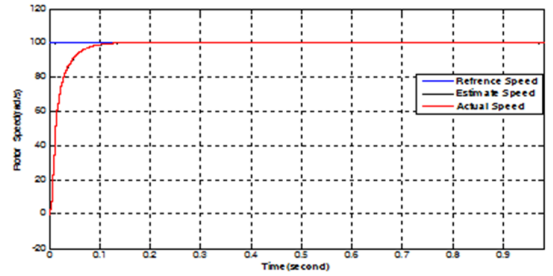
Figure 4. Block diagram of the proposed back-emf observer

V. SIMULATION RESULTS

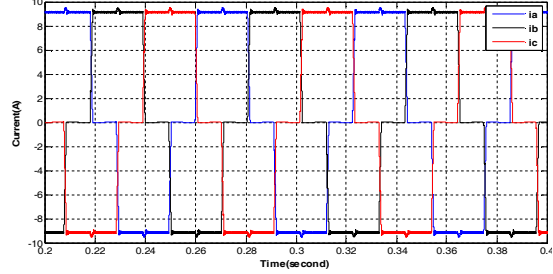
The simulation is carried out using MATLAB/Simulink. The parameters of BLDC motor used in simulations are given in table II. Firstly, under rated load torque, a reference speed of 100 rad/sec is assumed. The waveforms of speed, phase current and back-emf voltage are shown in Fig. 5. The speed estimation as well as speed tracking has a good response in steady state and in transient situations. Moreover, the phase current waveforms are near to ideal quasi-square.

TABLE II. BRUSHLESS DC MOTOR PARAMETER

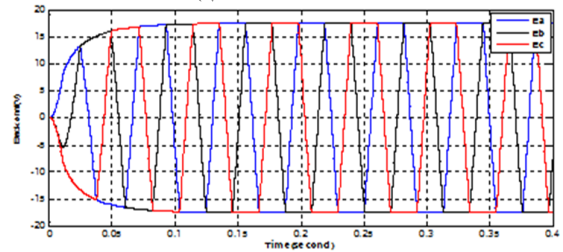
Number of poles	P	2
Rated speed	ω_{rated}	1500 RPM
Dc link voltage	V_{dc}	300 [V]
Self-inductance	L_s	13 [mH]
Phase resistance	R_s	0.4 [Ω]
Viscous damping coefficient	B	0.002 [N.m/(rad/sec)]
Moment of inertia	J	0.004 [kg.m ²]
Load torque	C	3 [N.m]
flux linkage	λ_m	0.175 v.s



(a) Speed tracking



(b) Current waveforms



(c) Back-emf voltage waveforms

Figure 5. Dynamic performance of the DPC based BLDC motor drive at speed reference of 100 rad/sec

Fig. 6 shows the dynamic response to variations of speed reference. The speed estimation and tracking is acceptable. The load torque is rated and as well as increasing of the speed, the motor power is rising.

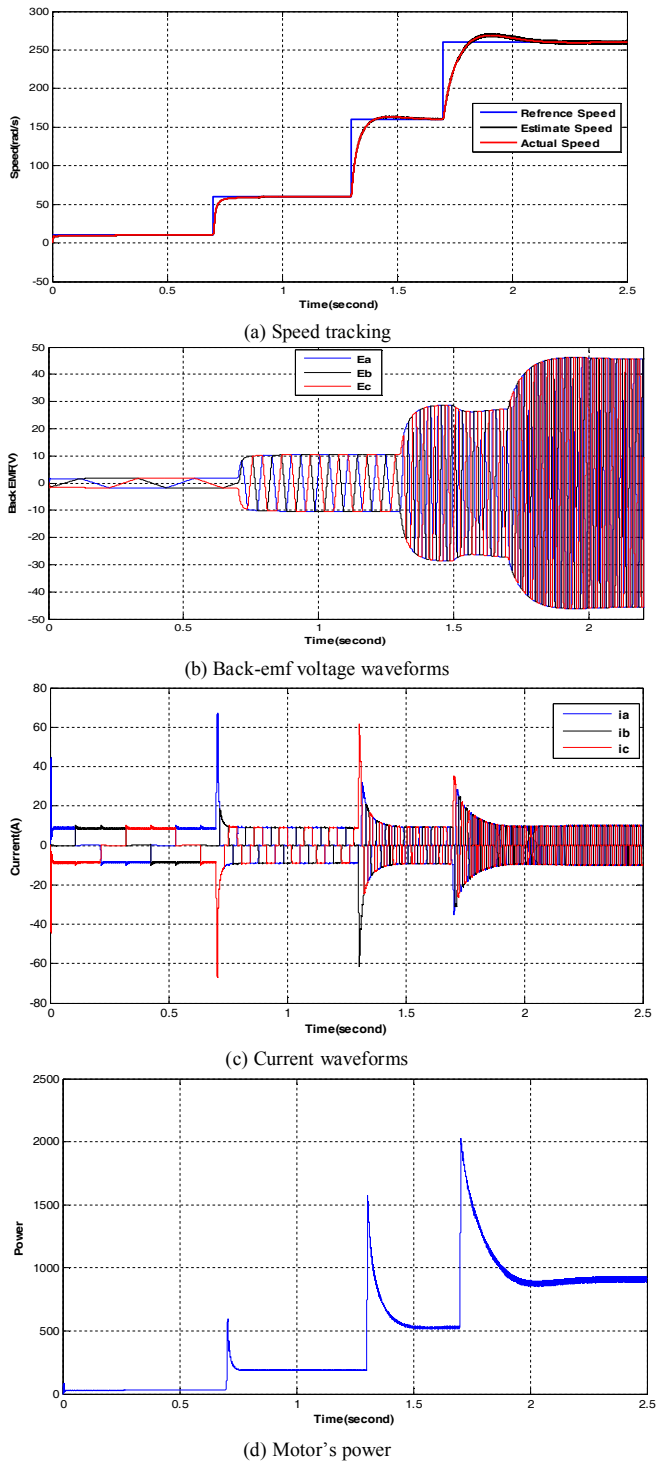


Figure 6. Dynamic response to step variations of speed reference

Fig. 7 shows the dynamic response to variation of load torque at speed reference of 100 rad/sec. Speed estimation and tracking is well done. Also power of the motor is increasing

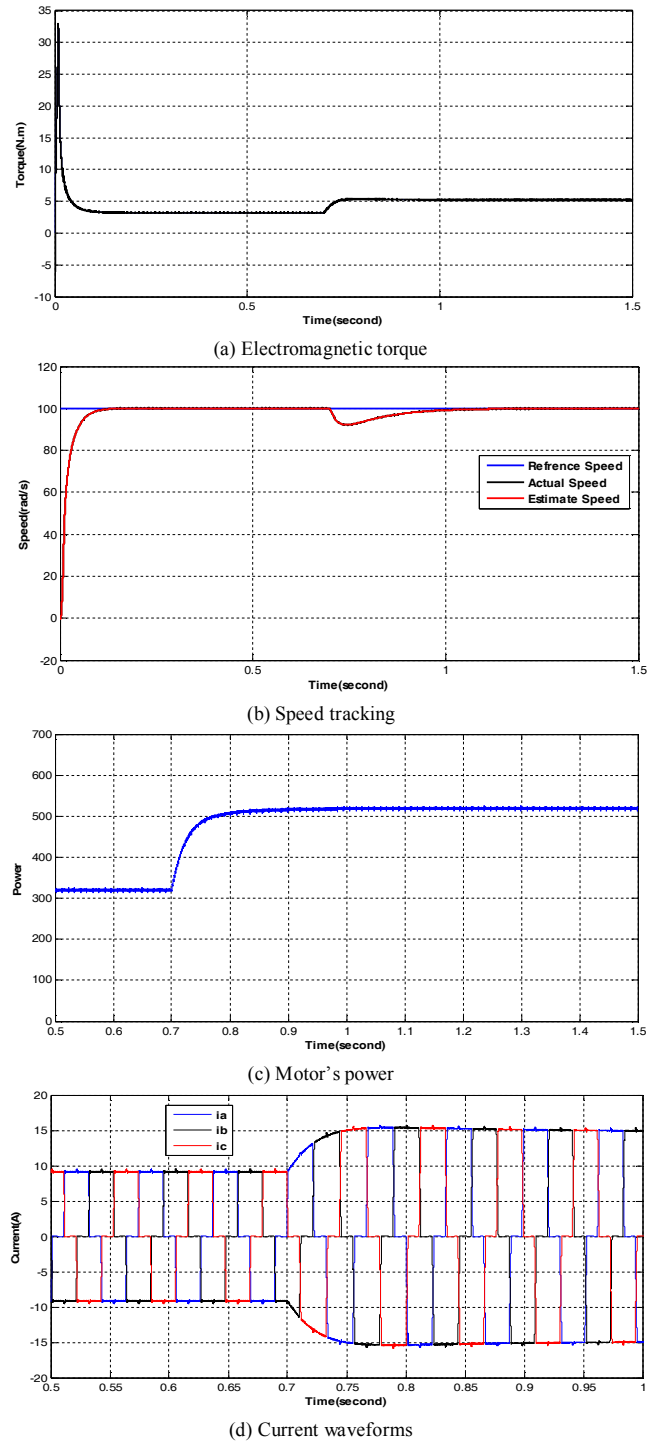


Figure 7. Dynamic response to step variation of load torque at speed of 100 rad/sec

VI. CONCLUSIONS

In this paper, the sensorless direct power control using the unknown input observer for controlling of BLDC motor has been studied. This observer can be obtained effectively by using the equation of augmented system and an estimated line-to-line back-emf that is modeled as an unknown input. As a result, the actual rotor position as well as the machine speed can be estimated strictly even in the transient state from the estimated line-to-line back-emf. The Simulation results show that this control scheme for BLDC motor has all the advantages of direct torque control. In addition, in this method sensitive to parameters is less. One of the major advantages of the DPC method compared to the DTC method that it is can be easily estimated actual power for control system.

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